Dr Walker's C of E Primary School

An Exceptional Place to Flourish

Though your beginning was small,
your future will flourish indeed.
Job 8:7

NON-STATUTORY POLICY	

Maths Calculations Policy	

Ratified by Governors	06.11.23
Review Cycle	Annually

Contents

Pre-amble: School Vision, Ethos and Values

Dr Walker's is a mixed Church of England Voluntary Controlled Primary School in Fyfield, Ongar, Essex.

Dr Walker's Church of England Primary School is a school where every child is loved, developed, and educated into becoming a successful British Citizen, through promoting the fundamental British values of:

- **Democracy**
- **The rule of law**
- **Individual liberty**
- **Mutual respect and**
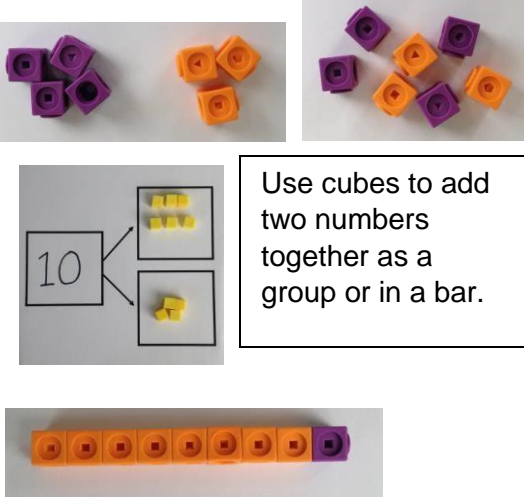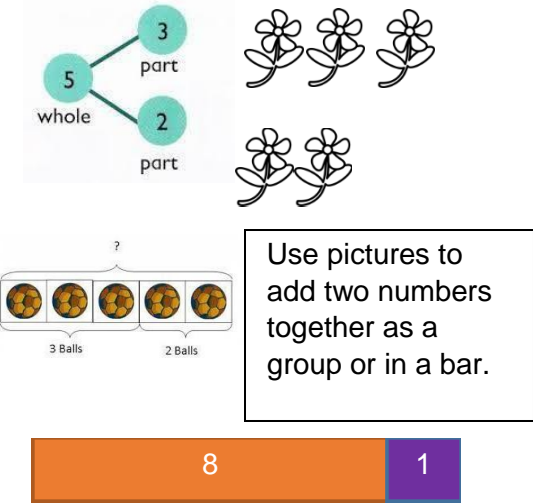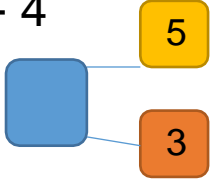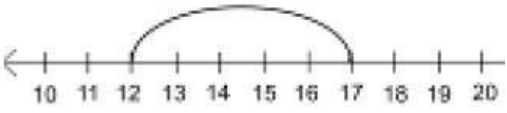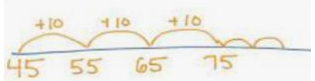- **Tolerance of those with different faiths and beliefs.**

We aspire that all pupils succeed in reaching their God given potential at Dr Walker's - An Exceptional Place to Flourish, by:

- **Believing** in God, self and others by developing confidence, respect and trust;
- **Engaging** in a love for learning by nurturing curiosity and independence; and
- **Excelling** in reaching personal potential by being resilient and showing positive behaviour.

Our **CHRISTIAN VALUES** are reflected in:

- *Standing with **COURAGE** for what is right.*
- *Using **CREATIVITY** in problem solving and making life beautiful.*
- *Treating every person and everything with **RESPECT**.*
- *Having **COMPASSION** for others.*
- *Completing every task with **PERSEVERANCE**.*
- *Taking **RESPONSIBILITY** for ourselves.*
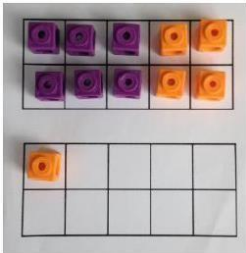- *Living with **HOPE** for a better future.*

Progression in Calculations Addition

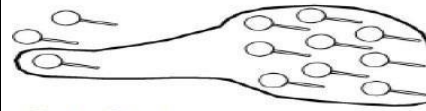| Objective and Strategies	Concrete	Pictorial	Abstract
Combining two parts to make a whole: part-whole model	Use cubes to add two numbers together as a group or in a bar.	Use pictures to add two numbers together as a group or in a bar.	$4 + 3 = 7$ $10 = 6 + 4$ Use the part-part whole diagram as shown above to move into the abstract.
Starting at the bigger number and counting on	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	$12 + 5 = 17$ Start at the larger number on the number line and count on in ones or in one jump to find the answer. This can progress to adding two 2-digit numbers. $45 + 32 = 77$	$5 + 12 = 17$ Place the larger number in your head and count on the smaller number to find your answer.

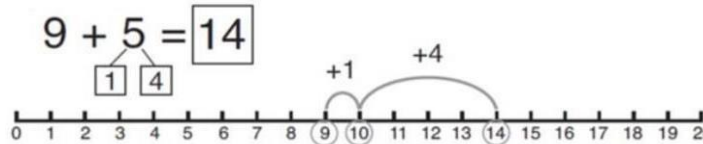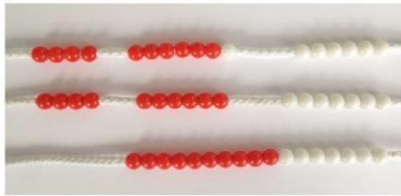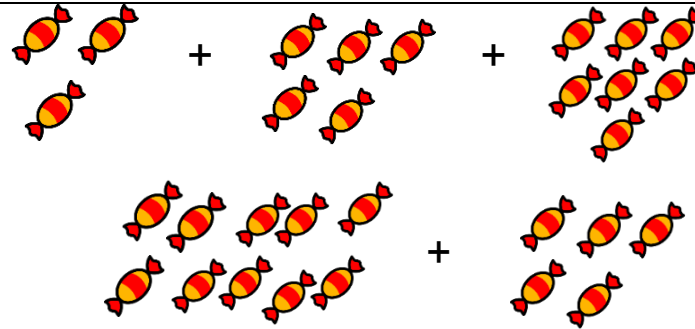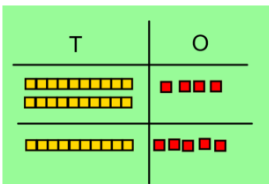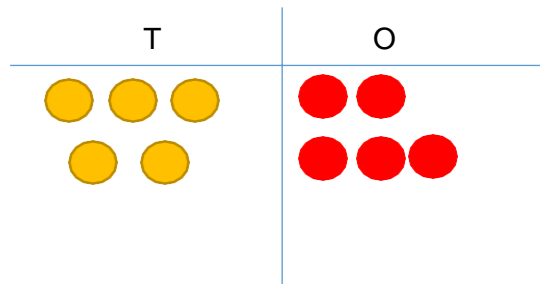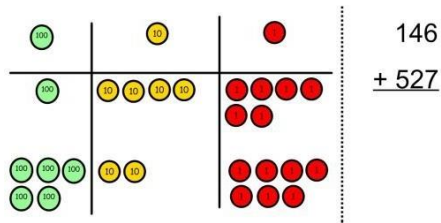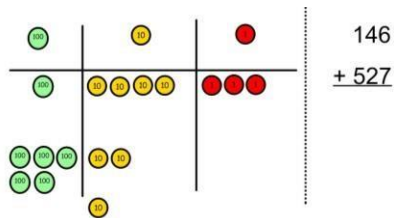|			
Regrouping to make 10.	 6 + 5 = 11 Start with the bigger number and use the smaller number to make 10.	Use pictures or a number line. Regroup or partition the smaller number to make 10. $9 + 5 = 14$ 1 4 	7 + 4= 11 If I am at seven, how many more do I need to make 10. How many more do I add on now?
Adding three single digits	4 + 7 + 6= 17 Put 4 and 6 together to make 10. Add on 7. Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.	 Add together three groups of objects. Draw a picture to recombine the groups to make 10.	$4 + 7 + 6 = 10 + 7$ 10 $= 17$ Combine the two numbers that make 10 and then add on the remainder.
Column method- no regrouping	24 + 15= Add together the ones first then add the tens, using Dienes (Base 10). 	After practically using the base 10 blocks and place value counters, children can draw base 10 apparatus – 'sticks and dots' or counters. 	Calculations 21 + 42 = 21 + 42

Column method- regrouping	Make both numbers on a place value grid.		Children can draw a pictoral representation of the columns and place value counters to further support their learning and understanding.	Start by partitioning the numbers before moving on to clearly show the exchange below the addition.

Make both numbers on a place value grid.

146
+ 527

Add up the units and exchange 10 ones for one 10.

146
+ 527

Add up the rest of the columns, exchanging the 10 counters from one column for the next place value column until every column has been added.

This can also be done with Base 10 to help children clearly see that 10 ones equal 1 ten and 10 tens equal 100.

As children move on to decimals, money and decimal place value counters can be used to support learning.

Children can draw a pictoral representation of the columns and place value counters to further support their learning and understanding.

7	1	5	1
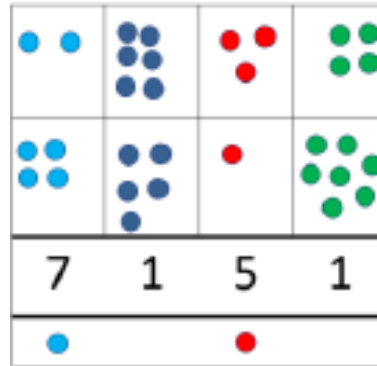
We also need to ensure that we use representations that include missing number values.

Start by partitioning the numbers before moving on to clearly show the exchange below the addition.

$$20 + 5$$
$$40 + 8$$
$$60 + 13 = 73$$
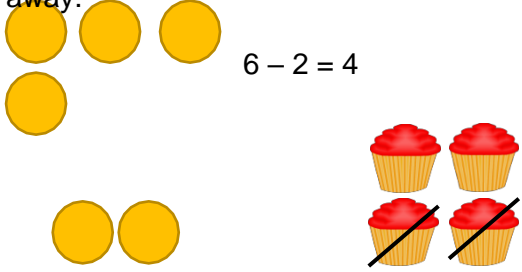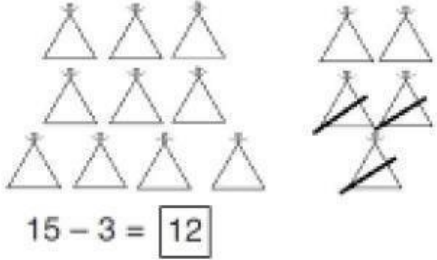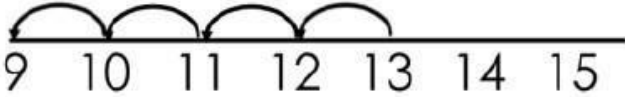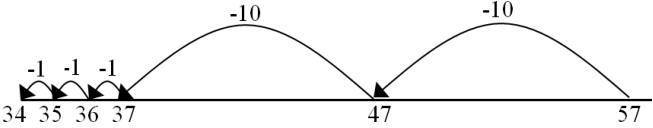
As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here.

536
+ 85
621
1 1

72.8
+ 54.6
127.4
1 1

£ 2 3 . 5 9
+ £ 7 . 5 5
£ 3 1 . 1 4
1 1   1

2 3 . 3 6 1
9 . 0 8 0
5 9 . 7 7 0
+ 1 . 3 0 0
9 3 . 5 1 1
2 1   2

Subtraction

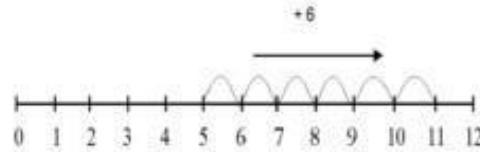| Objective and Strategies	Concrete	Pictorial	Abstract
Taking away ones	Use physical objects, counters, cubes etc to show how objects can be taken away. $6 - 2 = 4$	Cross out drawn objects to show what has been taken away. $15 - 3 = \boxed{12}$	$18 - 3 = 15$ $8 - 2 = 6$
Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. $13 - 4$ Use counters and move them away from the group as you take them away counting backwards as you go.	Count back on a number line or number track 9 10 11 12 13 14 15 Start at the bigger number and count back the smaller number showing the jumps on the number line. -10 -10 -1 -1 -1 34 35 36 37 47 57 This can progress all the way to counting back using two 2 digit numbers.	Put 13 in your head, count back 4. What number are you at? Use your fingers to help.

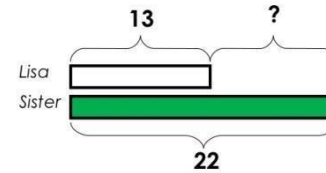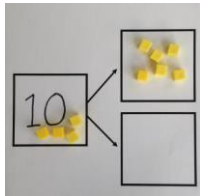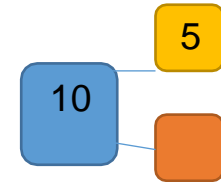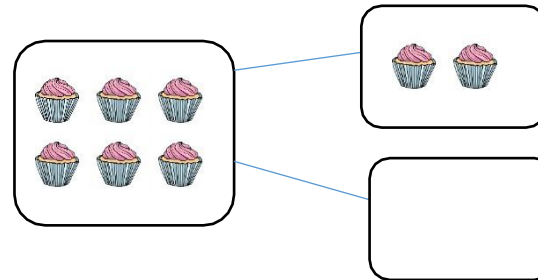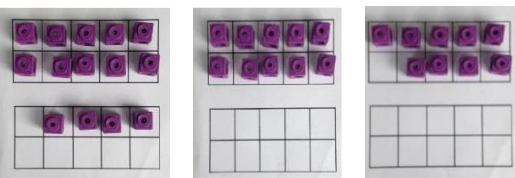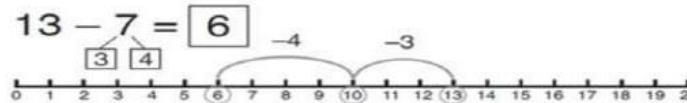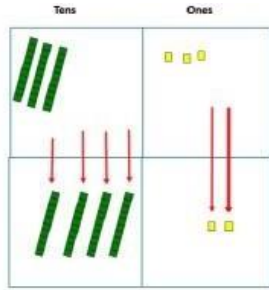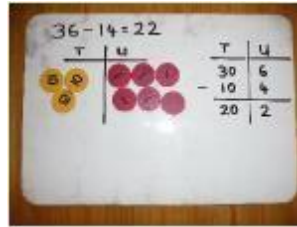|			
Find the difference	Compare amounts and objects to find the difference. Use cubes to build towers or make bars to find the difference 5 Pencils / 3 Erasers ? Use basic bar models with items to find the difference	+6 / 0 1 2 3 4 5 6 7 8 9 10 11 12 Draw bars to find the difference between 2 numbers. Count on to find the difference. **Comparison Bar Models** Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them. 13 ? Lisa / Sister 22	Hannah has 23 sandwiches, Helen has 15 sandwiches. Find the difference between the number of sandwiches. In previous column staff need to ensure that there is plenty of reference / practice to counting through tens.
Part Part Whole Model	10 Link to addition- use the part whole model to help explain the inverse between addition and subtraction. If 10 is the whole and 6 is one of the parts. What is the other part? 10 - 6 =	Use a pictorial representation of objects to show the part part whole model.	5 / 10 Move to using numbers within the part whole model.
Make 10	14 – 9 = Make 14 on the ten frame. Take away the four first to make 10 and then takeaway one more so you have taken away 5. You are left with the answer of 9.	$13 - 7 = \boxed{6}$ −4 −3 / 3 4 / 0 1 2 3 4 5 (6) 7 8 9 (10) 11 12 (13) 14 15 16 17 18 19 20 Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.	16 – 8= How many do we take off to reach the next 10? How many do we have left to take off?

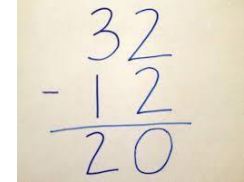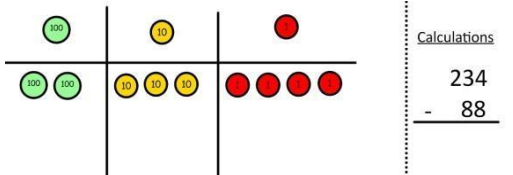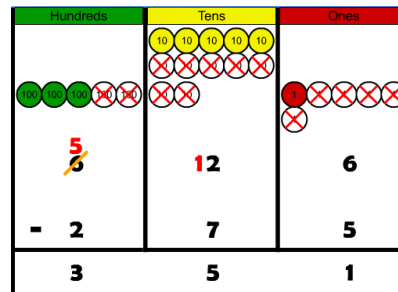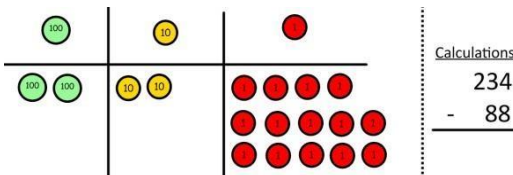| Column method without regrouping				
	Show how you partition numbers to subtract. Again make the larger number first.	Use Base 10 to make the bigger number then take the smaller number away.	Draw the Base 10 or place value counters alongside the written calculation to help to show working. Emphasise the value of the digit e.g. 4 tens	Previous policy had a partition version. We do not see the value in this. This will lead to a clear written column subtraction.

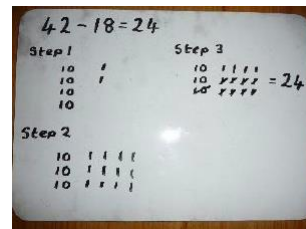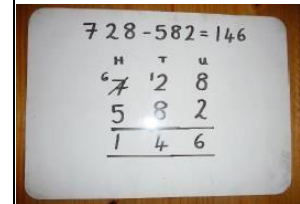| Column method with regrouping				
	Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges. Make the larger number with the place value counters Start with the ones, can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones.	and knows when to exchange/regroup.	Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make. When confident, children can find their own way to record the exchange/regrouping. Just writing the numbers as shown here shows that the child understands the method	Children can start their formal written method by partitioning the number into clear place value columns. Moving forward the children use a more compact method.

Now I can subtract my ones.

Calculations
234
- 88
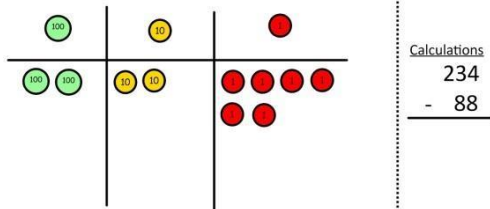
Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.

Calculations
234
- 88
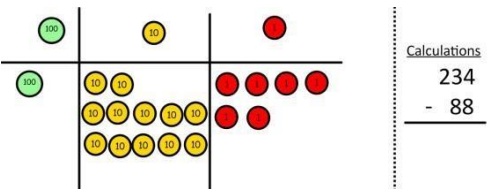
Now I can take away eight tens and complete my subtraction
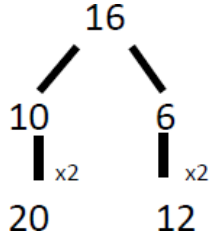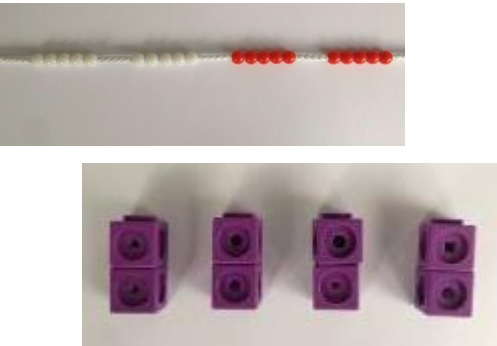

Calculations
¹2̸3̷4
- 88
146
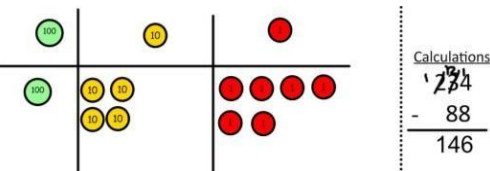
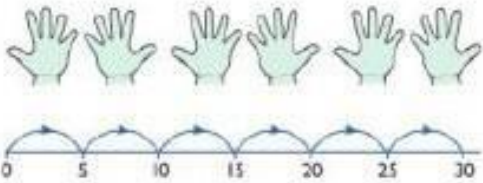Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.

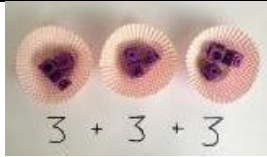This will lead to an understanding of subtracting any number including decimals.

$$
\begin{array}{r}
\;\;5\;\;12\;\;\;1 \\
2\;\;\not{6}\;\;\not{3}\;.\;\;\textbf{0} \\
-\;\;\;2\;\;6\;.\;\;5 \\
\hline
2\;\;3\;\;6\;.\;\;5
\end{array}
$$

Multiplication

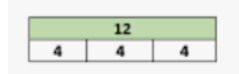| Objective and Strategies	Concrete	Pictorial	Abstract
Doubling	Use practical activities to show how to double a number.	Draw pictures to show how to double a number. Double 4 is 8 	16 10 6 x2 x2 20 12 Partition a number and then double each part before recombining it back together.
Counting in multiples	 Count in multiples supported by concrete objects in equal groups.	 Use a number line or pictures to continue support in counting in multiples.	Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25 , 30

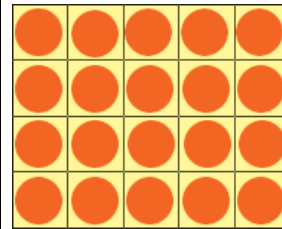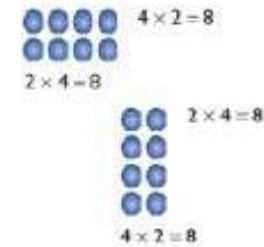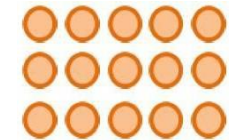|			
Repeated addition	3 + 3 + 3 Use different objects to add equal groups.	There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there? 2 add 2 add 2 equals 6 $5 + 5 + 5 = 15$ Use of a bar model	Write addition sentences to describe objects and pictures. $2 + 2 + 2 + 2 + 2 = 10$
Arrays- showing commutative multiplication	Create arrays using counters/ cubes to show multiplication sentences.	Draw arrays in different rotations to find **commutative** multiplication sentences. $4 \times 2 = 8$ $2 \times 4 = 8$ $2 \times 4 = 8$ $4 \times 2 = 8$ Link arrays to area of rectangles. Teachers should also use bar model. E.g Whole =20 and below are five parts of 4.	Use an array to write multiplication sentences and reinforce repeated addition. $5 + 5 + 5 = 15$ $3 + 3 + 3 + 3 + 3 = 15$ $5 \times 3 = 15$ $3 \times 5 = 15$
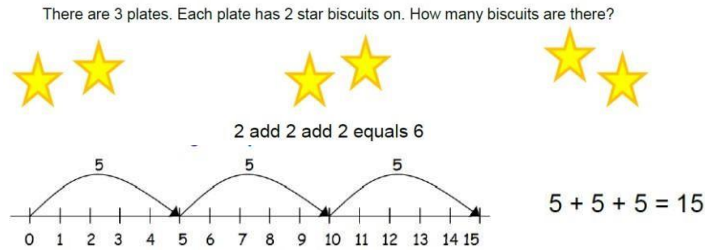
Grid Method

This can be shown on initial introduction and used for those whose place value is less secure but pupils should move on reasonably quickly to column method.

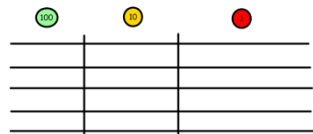Show the link with arrays to first introduce the grid method.

x	10	3
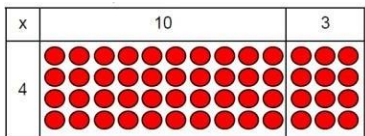
4 rows of 10
4 rows of 3

Move on to using Base 10 to move towards a more compact method.
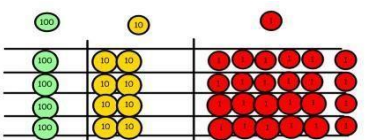

x	T	U
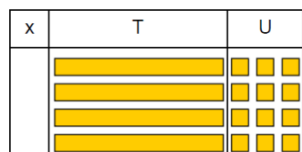
4 rows of 13

Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows.
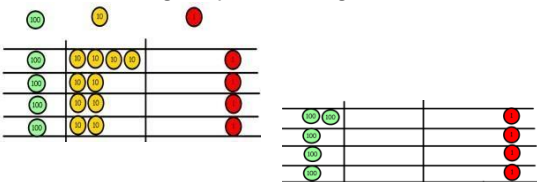

Calculations
4 x 126

Fill each row with 126.

Calculations
4 x 126

Add up each column, starting with the ones making any exchanges needed.

Then you have your answer.

Children can represent the work they have done with place value counters in a way that they understand.

They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.
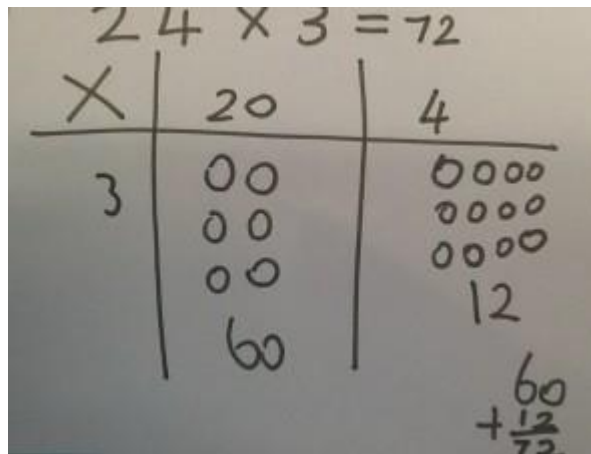
Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

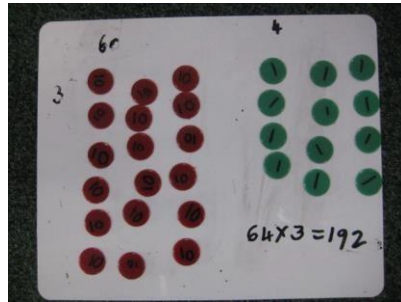| ×	30	5
7	210	35

210 + 35 = 245

Moving forward, multiply by a 2 digit number showing the different rows within the grid method.
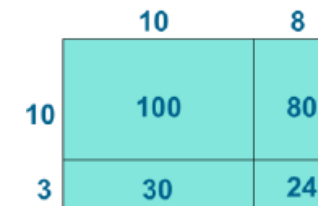
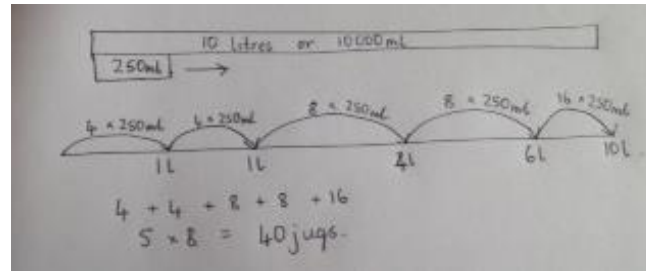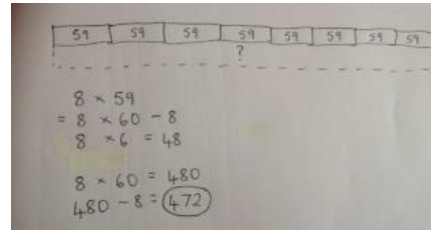| X	1000	300	40	2
10	10000	3000	400	20
8	8000	2400	320	16

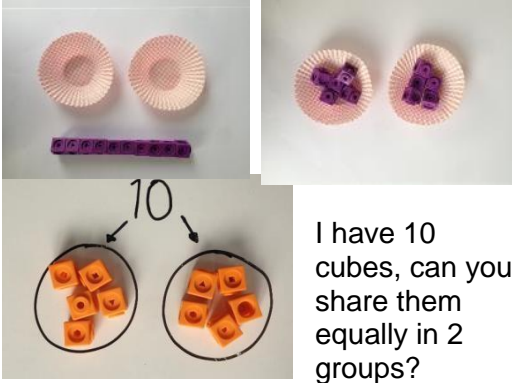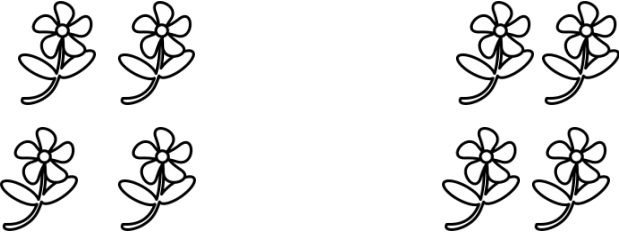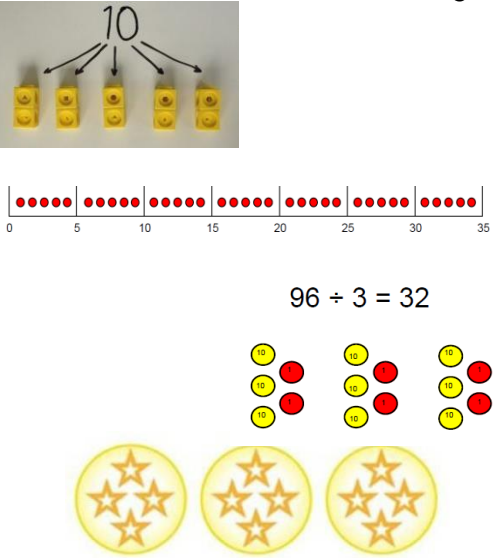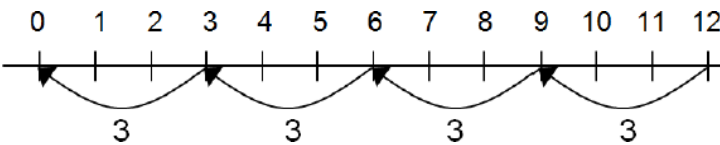| Column multiplication	Children can continue to be supported by place value counters at the stage of multiplication.	Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.	Start with long multiplication, reminding the children about lining up their numbers clearly in columns.
	$64 \times 3 = 192$	8×59 $= 8 \times 60 - 8$ $8 \times 6 = 48$ $8 \times 60 = 480$ $480 - 8 = (472)$	If it helps, children can write out what they are solving next to their answer.
	It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below.	10 Litres or 10000 mL $4 + 4 + 8 + 8 + 16$ $5 \times 8 = 40 \text{ jugs}$	$\begin{array}{r} 32 \\ \times\ 24 \\ \hline 8 \quad (4 \times 2) \\ 120 \quad (4 \times 30) \\ 40 \quad (20 \times 2) \\ 600 \quad (20 \times 30) \\ \hline 768 \end{array}$
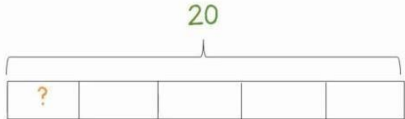
$$\begin{array}{cccc} & & 7 & 4 \\ \times & & 6 & 3 \\ \hline & & 1 & 2 \\ & 2 & 1 & 0 \\ & 2 & 4 & 0 \\ + 4 & 2 & 0 & 0 \\ \hline 4 & 6 & 6 & 2 \end{array}$$

This moves to the more compact method.
NB – When calculating do the ones first and then the tens. Opposite to model below.

$$\begin{array}{r} {}^{2}\ {}^{3}\ {}^{1} \\ 1\,3\,4\,2 \\ \times \quad 1\,8 \\ \hline 1\,3\,4\,2\,0 \\ 1\,0\,7\,3\,6 \\ \hline 2\,4\,1\,5\,6 \\ {}_{1} \end{array}$$

Division

Objective and Strategies	Concrete	Pictorial	Abstract
Sharing objects into groups	 I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities. $$8 \div 2 = 4$$	Share 9 buns between three people. $$9 \div 3 = 3$$
Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding. $$96 \div 3 = 32$$ 	Use a number line to show jumps in groups. The number of jumps equals the number of groups. Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group. $20 \div 5 = ?$ $5 \times ? = 20$	$28 \div 7 = 4$ Divide 28 into 7 groups. How many are in each group?

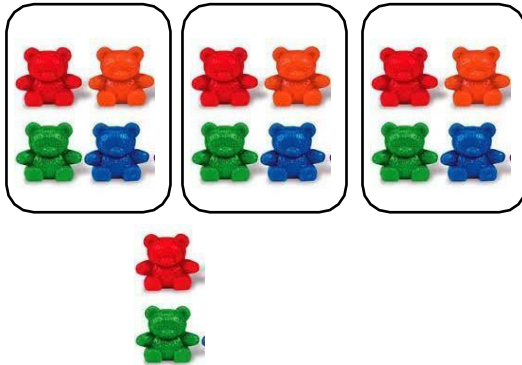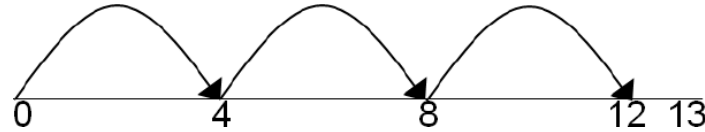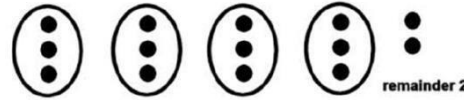|			
Division within arrays	Link division to multiplication by creating an array and thinking about the number sentences that can be created. Eg 15 ÷ 3 = 5 5 x 3 = 15 15 ÷ 5 = 3 3 x 5 = 15	 Draw an array and use lines to split the array into groups to make multiplication and division sentences.	Find the inverse of multiplication and division sentences by creating four linking number sentences. 7 x 4 = 28 4 x 7 = 28 28 ÷ 7 = 4 28 ÷ 4 = 7
Division with a remainder	14 ÷ 3 = Divide objects between groups and see how much is left over 	Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder. Draw dots and group them to divide an amount and clearly show a remainder. 	Complete written divisions and show the remainder using r. 29 ÷ 8 = 3 REMAINDER 5 ↑ ↑ ↑ ↑ dividend divisor quotient remainder
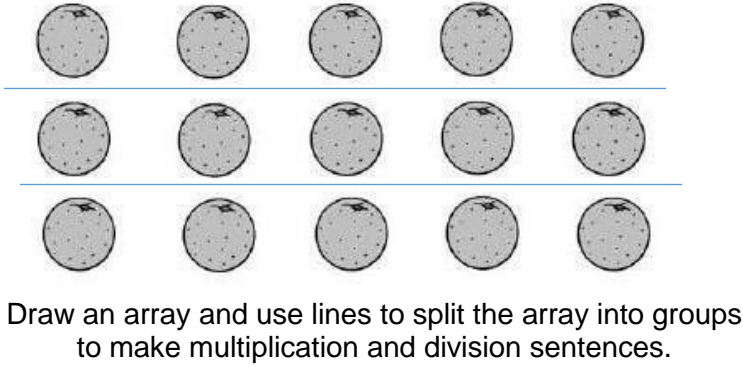
Short division

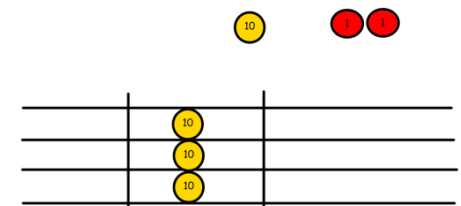**Tens**   **Units**

3   2

3
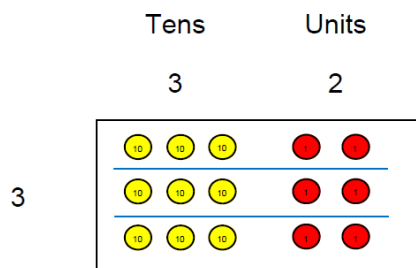
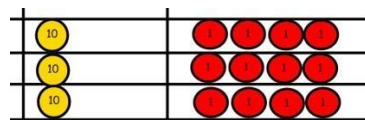Use place value counters to divide using the bus stop method alongside

Calculations

42 ÷ 3
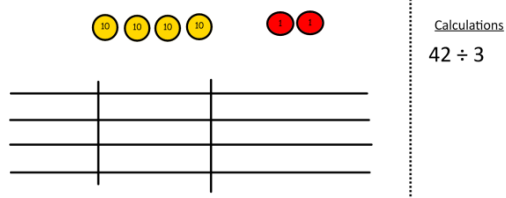
42 ÷ 3=
Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.
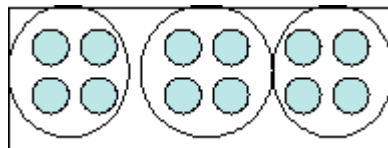

We exchange this ten for ten ones and then share the ones equally among the groups.

We look how much in 1 group so the answer is 14.

Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.

Encourage them to move towards counting in multiples to divide more efficiently.

NB – Where possible pupils should be given a context for division .e.g. sweets divided amongst a group of friends, a bill shared by a group of adults.
This gives a context for the type of remainder e.g whole number , decimal etc.

Begin with divisions that divide equally with no remainder.

```
    2  1  8
          3
4 | 8  7  2
```

Move onto divisions with a remainder.

```
    8  6   r 2
          3
5 | 4  3  2
```

Finally move into decimal places to divide the total accurately.

```
       1  4  .  6
             16    21
3  5 | 5  1  1  .  0
```
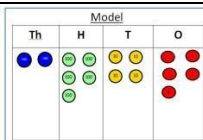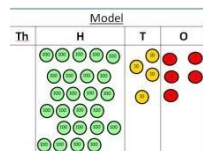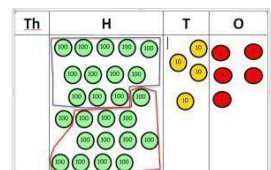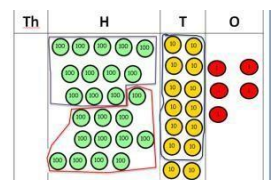
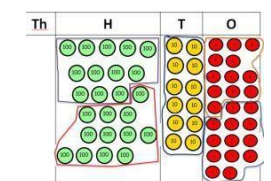| Long division	2544 ÷ 12 How many groups of 12 thousands do we have? None	Instead of using physical counters, students can draw the counters and circle the groups on a whiteboard or in their books.	
	Exchange 2 thousand for 20 hundreds. $$\begin{array}{r} 0 \\ 12\overline{\smash{)}2\overset{2}{5}44} \end{array}$$	Use this method to explain what is happening and as soon as they have understood what move on to the abstract method as this can be a time consuming process.	
	How many groups of 12 are in 25 hundreds? 2 groups. Circle them. We have grouped 24 hundreds so can take them off and we are left with one. $$\begin{array}{r} 0\ 2 \\ 12\overline{\smash{)}2\overset{2}{5}44} \\ \underline{24} \\ 1 \end{array}$$		
	Exchange the one hundred for ten tens so now we have 14 tens. How many groups of 12 are in 14? 1 remainder 2 $$\begin{array}{r} 0\ 2\ 1 \\ 12\overline{\smash{)}2\overset{2}{5}4\overset{2}{4}} \\ \underline{24} \\ 14 \\ \underline{12} \\ 2 \end{array}$$		
	Exchange the two tens for twenty ones so now we have 24 ones. How many groups of 12 are in 24? 2 $$\begin{array}{r} 0\ 2\ 1\ 2 \\ 12\overline{\smash{)}2\overset{2}{5}4\overset{2}{4}} \\ \underline{24} \\ 14 \\ \underline{12} \\ 24 \\ \underline{24} \\ 0 \end{array}$$		